

Molecular Oxygen-Induced Ferromagnetism and Half-Metallicity in  $\alpha$ -BaNaO<sub>4</sub>: A First-Principles Study

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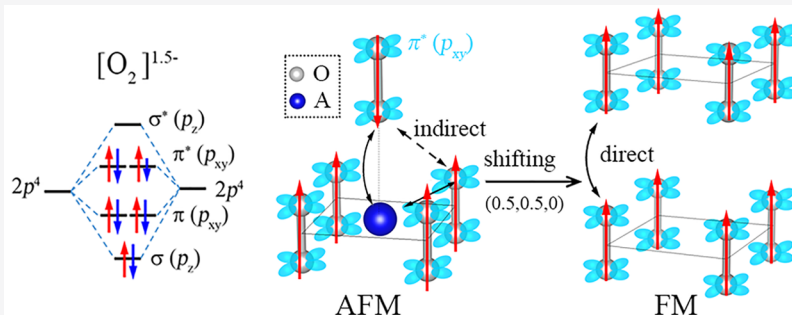
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**ABSTRACT:** Molecular oxygen resembles 3d and 4f metals in exhibiting long-range spin ordering and strong electron correlation behaviors in compounds. Ferromagnetic spin ordering and half-metallicity, however, are quite elusive and have not been well acknowledged. In this Article, we address this issue by studying how spins will interact with each other if the oxygen dimers are arranged in a different way from that in the known superoxides and peroxides by first-principles calculations. Based on the results of a structure search, thermodynamic studies, and lattice dynamics, we show that tetragonal  $\alpha$ -BaNaO<sub>4</sub> is a stable half-metal with a Curie temperature at 120 K, the first example in this class of compounds. Like 3d and 4f metals, the O<sub>2</sub> dimer carries a local magnetic moment of 0.5  $\mu_B$  due to the unpaired electrons in its  $\pi^*$  orbitals. This compound can be regarded as forming from the O<sub>2</sub> dimer layers stacking in a head-to-head way. In contrast to the arrangement in AO<sub>2</sub> (A = K, Rb, Cs), the spins are ferromagnetically coupled both within and between the layers. Spin polarization occurs in  $\pi^*$  orbitals, with spin-up electrons fully occupying the valence band and spin-down electrons partially occupying the conduction band, forming semiconducting and metallic channels, respectively. Our results highlight the importance of geometric arrangement of O<sub>2</sub> dimers in inducing ferromagnetism and other novel properties in O<sub>2</sub>-dimer-containing compounds.

## ■ INTRODUCTION

Molecular oxygen (O<sub>2</sub>) has long been known to carry a local moment because of the existence of unpaired electron in its  $\pi^*$  orbitals.<sup>1</sup> When condensing into a solid at low temperatures (~24 K), it exhibits a long-range antiferromagnetic (AFM) ordering.<sup>2,3</sup> Alkali metal superoxides (O<sub>2</sub><sup>•−</sup>), peroxides (O<sub>2</sub><sup>2−</sup>), and dioxygenyl (O<sub>2</sub><sup>+</sup>) salts all contain molecular oxygen but with different numbers of electrons in their  $\pi^*$  orbitals, leading to a variety of magnetic properties. Typical examples are AFM AO<sub>2</sub> (A = Na, K, Rb, Cs),<sup>4–9</sup> spin-glass Rb<sub>4</sub>O<sub>6</sub>/Cs<sub>4</sub>O<sub>6</sub>,<sup>10,11</sup> ferrimagnetic (FiM) O<sub>2</sub>PtF<sub>6</sub>,<sup>12,13</sup> and paramagnetic O<sub>2</sub>SbF<sub>6</sub>.<sup>13</sup> Long-range ferromagnetic (FM) ordering, however, is quite elusive in these O<sub>2</sub>-dimer-containing compounds, though many attempts have been made to study it over the past decades.

A weak ferromagnetism was reported in Ba<sub>1−x</sub>K<sub>x</sub>O<sub>2</sub> for  $x = 0.269$ , and a spin-glass behavior for other K doping levels, which were ascribed to the coexistence of and the competition between AFM and FM.<sup>14,15</sup> Partial oxygen deficiency at  $x = 0.28$  in RbO<sub>2−x</sub> was found to result in a transition from AFM

to spin-glass, and presumably there is short-range FM ordering in clusters at ~50 K.<sup>16</sup> Theoretically, the electrons in the  $\pi^*$  orbitals of O<sub>2</sub> dimers can be better treated as a strongly correlated system.<sup>17,18</sup> Naghavi et al. predicted that pressure would make Rb<sub>4</sub>O<sub>6</sub> transform from an AFM insulator to an FM insulator then to an FM half-metal, which is a consequence of Mott transitions.<sup>19</sup> It is argued from first-principles calculations that anionogenic ferromagnetism and half-metallicity will emerge at the interface of KO<sub>2</sub>/BaO<sub>2</sub> through double-exchange interactions of O<sub>2</sub><sup>2−</sup> and O<sub>2</sub><sup>•−</sup>.<sup>20</sup> A question arises: Is long-range FM ordering possible in a bulky molecular oxygen-containing compound, as it is in a 3d metal counterpart? If so, can a half-metal be evolved from the

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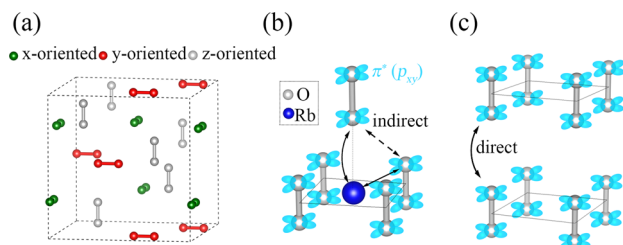
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ferromagnetism? This is of importance in further understanding the interaction behavior among these local moments carried by O<sub>2</sub> dimers.

To begin, we first show the importance of O<sub>2</sub> dimer orientation in inducing long-range ordering by taking Rb<sub>4</sub>O<sub>6</sub> and RbO<sub>2</sub> as examples; see Figure 1a,b. The O<sub>2</sub> dimers in



**Figure 1.** (a) Sketch of arrangement of O<sub>2</sub> dimers in Rb<sub>4</sub>O<sub>6</sub>. For simplification, all the cations are omitted. (b, c) Orbital-based schematic diagrams of (b) indirect magnetic interaction between the O<sub>2</sub> dimers in RbO<sub>2</sub> and (c) hypothetical direct magnetic interaction between the O<sub>2</sub> dimers. The magnetic interactions originate from the unfilled  $\pi^*(p_{xy})$  orbitals (blue).

Rb<sub>4</sub>O<sub>6</sub> align on three principal axes. Due to geometric frustration, it does not show long-range magnetic ordering.<sup>10</sup> In contrast, the ground state of RbO<sub>2</sub> is experimentally confirmed to be AFM,<sup>5</sup> for all the O<sub>2</sub> dimers align parallel. The O<sub>2</sub> dimers couple ferromagnetically in the (001) planes in RbO<sub>2</sub> while interacting antiferromagnetically between adjacent planes with a relative shift of (0.5a, 0.5a, 0), where a is the lattice parameter. Both magnetic exchange interactions are theoretically found to be indirect, i.e., via the cations through superexchange.<sup>21</sup> The same is true for AFM KO<sub>2</sub> and CsO<sub>2</sub>.<sup>4</sup> These facts suggest that the O<sub>2</sub> dimer layers in such a stacking way favor the AFM interlayer exchange interactions for local moments. Recent studies showed that changes in the relative orientation of layers will give rise to tremendous changes in electronic properties and hence result in emergent phenomena.<sup>22</sup> We try to apply this idea to the O<sub>2</sub>-dimer-containing compounds to explore how their magnetic properties will change—specifically, rearranging the relative orientation of

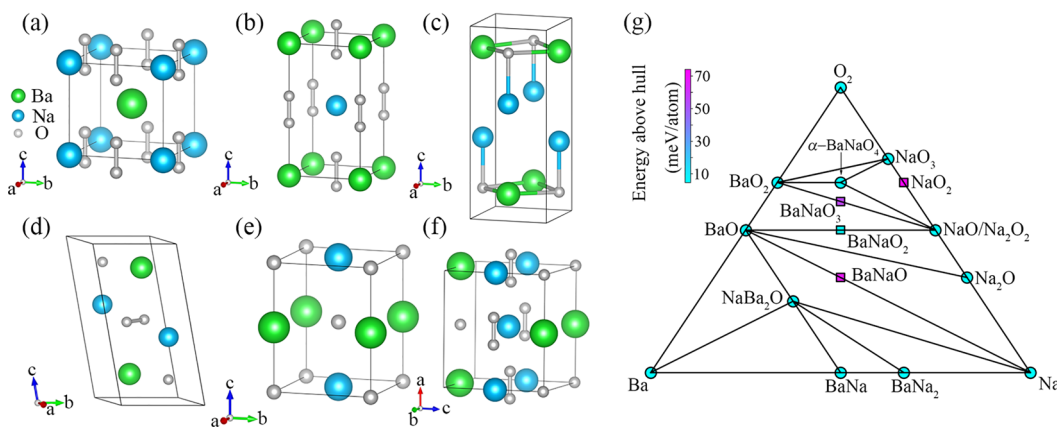
neighboring O<sub>2</sub> dimer layers while keeping the intralayer unchanged. Figure 1c shows a possible simple solution, where the O<sub>2</sub> dimers stack along the [001] direction in a head-to-head way. In this way, the O<sub>2</sub> dimers in neighboring planes are expected to have direct exchange interactions and bring about very different magnetic properties.

Since no known binary peroxides and superoxides have such an O<sub>2</sub> arrangements in their structures, ternary compounds should be considered. However, very few ternary peroxides or superoxides have been reported so far. The substitution of K for Ba in BaO<sub>2</sub> only leads to a solid solution, without changing the structure type.<sup>14</sup> This is not beyond expectation, since K<sup>+</sup> ion and Ba<sup>2+</sup> ion are comparable in size. The desired structure is more likely to form if a smaller ion, say Na<sup>+</sup>, is used instead.

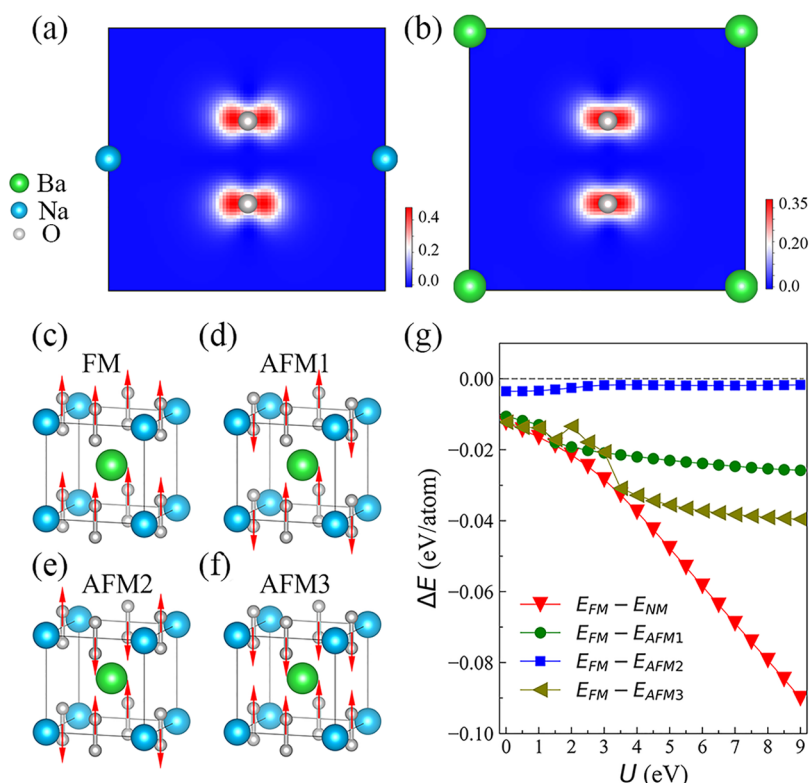
In this Article, we report attempts to identify  $\alpha$ -BaNaO<sub>4</sub> in which the O<sub>2</sub> dimers arrange in the way shown in Figure 1c among the predicted compounds by performing a systematic structure search. This compound is stable in terms of formation enthalpy, mechanical dynamics, and lattice dynamics. It exhibits ferromagnetism and half-metallicity, with a large spin gap  $\sim 4$  eV (HSE06) in the ground state. The emergent half-metallicity is attributed to the partial occupation of the O<sub>2</sub> dimer  $\pi^*$  bonds, which leads to the spin splitting. Monte Carlo simulations based on the Heisenberg model indicate that the spin ordering occurs at a Curie temperature ( $T_c$ ) of 120 K. Our results show that compounds with adjacent O<sub>2</sub> dimer layers stacking in a head-to-head way are possible and may change the interlayer coupling from AFM to FM, highlighting the importance of the relative shift of adjacent layers in inducing novel properties for this category of compounds.

## COMPUTATIONAL DETAILS

First-principles calculations were carried out with the density functional theory (DFT) implemented in the Vienna *ab initio* simulation package (VASP).<sup>23</sup> We adopted the generalized gradient approximation (GGA) in the form of Perdew–Burke–Ernzerhof (PBE)<sup>24</sup> for the exchange–correlation potentials. The projector-augmented-wave (PAW)<sup>25</sup> pseudopotentials were used with a plane wave energy of 680 eV; 2s<sup>2</sup>2p<sup>4</sup>, 2p<sup>6</sup>3s<sup>1</sup>, and 5s<sup>2</sup>5p<sup>6</sup>6s<sup>2</sup> were treated as valence electrons for O, Na, and Ba, respectively. A Monkhorst–Pack<sup>26</sup> Brillouin zone sampling grid with a resolution 0.02  $\times 2\pi$  Å<sup>−1</sup> was applied. Atomic positions and lattice parameters were relaxed



**Figure 2.** Crystal structures of (a)  $P4/mmm$ -BaNaO<sub>4</sub> ( $\alpha$ -BaNaO<sub>4</sub>), (b)  $P4/mmm$ -BaNaO<sub>4</sub> ( $\beta$ -BaNaO<sub>4</sub>), (c)  $P4/nmm$ -BaNaO, (d)  $P1$ -BaNaO<sub>2</sub>, (e)  $P4/mmm$ -BaNaO<sub>2</sub>, and (f)  $Pmmn$ -BaNaO<sub>3</sub>. Green balls represent barium, blue ones sodium, and gray dumbbells O<sub>2</sub> dimer. (g) Phase diagram based on convex hull analysis of formation enthalpies for the Ba–Na–O system at  $T = 0$  K. Formation enthalpy  $\Delta H$  was defined as  $\Delta H_{\text{Ba}_x\text{Na}_y\text{O}_z} = E_{\text{Ba}_x\text{Na}_y\text{O}_z} - xE_{\text{Ba}} - yE_{\text{Na}} - (z/2)E_{\text{O}_2}$ , where  $E_{\text{Ba}_x\text{Na}_y\text{O}_z}$ ,  $E_{\text{Ba}}$ ,  $E_{\text{Na}}$ , and  $E_{\text{O}_2}$  are the total energies for Ba<sub>x</sub>Na<sub>y</sub>O<sub>z</sub>, bcc-Ba, bcc-Na, and  $\alpha$ -O<sub>2</sub>, respectively. The cyan circles indicate stable structures, while squares indicate metastable/unstable.



**Figure 3.** Magnetic density (electron/ $\text{\AA}^3$ ) of  $\alpha$ -BaNaO<sub>4</sub> (a) (100) plane and (b) (200) plane. The magnetic density  $\rho_{\text{mag}}$  is defined as  $\rho_{\text{mag}} = \rho_{\text{up}} - \rho_{\text{down}}$ , where  $\rho_{\text{up}}$  is the charge density of spin-up electrons and  $\rho_{\text{down}}$  the charge density of spin-down electrons. (c–f) Four possible collinear magnetic configurations. (g) Energy differences between the FM and AFM1, AFM2, AFM3, and NM configurations as a function of  $U$ .

until all the forces on the ions were less than  $10^{-4}$  eV/ $\text{\AA}$ . The DFT+ $U$  method was used where mentioned. The Hubbard  $U$  is applied to the O- $p$  orbitals. Phonon spectra were calculated using the finite displacement method implemented in the PHONOPY code<sup>27</sup> to determine the lattice dynamical stability of the structures. *Ab initio* molecular dynamics (AIMD) simulations were performed as implemented in VASP. The time step was chosen as 3 fs, and the duration was 9 ps. The hybrid functional HSE06 with a mixing parameter of 25% for the exact-exchange term was used to estimate the band gap in half-metals. We used the code from the Henkelman group<sup>28</sup> for Bader charge analysis. Structure searching and prediction were performed by using the particle swarm optimization (PSO) technique implemented in the CALYPSO code<sup>29</sup> in the Ba–Na–O system with molar ratio Ba:Na = 1:1.

## RESULTS AND DISCUSSION

A structure search was performed on BaNaO <sub>$x$</sub>  ( $x = 1–4$ ). The corresponding structures with low energy and reasonable coordination geometry were singled out as candidates for further investigations. This yielded  $P4/mmm$ - $\alpha$ -BaNaO<sub>4</sub>,  $P4/mmm$ - $\beta$ -BaNaO<sub>4</sub>,  $P4/nmm$ -BaNaO,  $P1$ -BaNaO<sub>2</sub>,  $P4/mmm$ -BaNaO<sub>2</sub>, and  $Pmnn$ -BaNaO<sub>3</sub>; see Figure 2a–f. We note that  $P4/nmm$ -BaNaO and  $P4/mmm$ -BaNaO<sub>2</sub> contain only O<sup>2–</sup>, and  $P1$ -BaNaO<sub>2</sub> and BaNaO<sub>3</sub> have both O<sub>2</sub> dimers and O<sup>2–</sup>, and  $\alpha$ - and  $\beta$ -BaNaO<sub>4</sub> have only O<sub>2</sub> dimers.  $\beta$ -BaNaO<sub>4</sub> resembles BaO<sub>2</sub> in structure except for the Ba at the body center being substituted by Na, which is added for comparison.  $\alpha$ -BaNaO<sub>4</sub> can be regarded as an O<sub>2</sub>-dimer-deficient perovskite with a zero occupation of the dimer in the Ba layer. The O<sub>2</sub> dimers form a layer by bonding with Na<sup>+</sup> ions in the (001) plane, and the layers stack in a head-to-head way along the [001] direction, separated by Ba<sup>2+</sup> ions. We notice that O-deficient perovskites are often seen in Cu-based superconductors.

Convex hull analyses of formation enthalpy were then performed to check the stability of these compounds by comparison with the known compounds in the Ba–Na–O ternary system. Figure 2g shows the calculated phase diagram. Only  $\alpha$ -BaNaO<sub>4</sub> is stable in terms of formation energy. Others lie above the convex hull, suggesting they are unstable or metastable. We further explore the behavior of  $\alpha$ -BaNaO<sub>4</sub> in terms of the lattice's dynamic, mechanical, and thermal stability. As there are no negative frequencies in the calculated phonon spectrum, its lattice is dynamically stable; see Figure S1 (Supporting Information, SI). For a stable compound, its elastic stiffness constants should satisfy the Born stability criteria.<sup>30</sup> The calculated stiffness values of  $\alpha$ -BaNaO<sub>4</sub> are found to well guarantee the demand of mechanical stability (see details in the SI). Furthermore, the structural stability at 500 K was examined through AIMD. During the simulation process (0–9 ps), the structure is well preserved in the framework of the Nosé–Hoover thermostat ensemble; see Figure S2 (SI). Hence, the structure of  $\alpha$ -BaNaO<sub>4</sub> is at least stable up to 500 K.

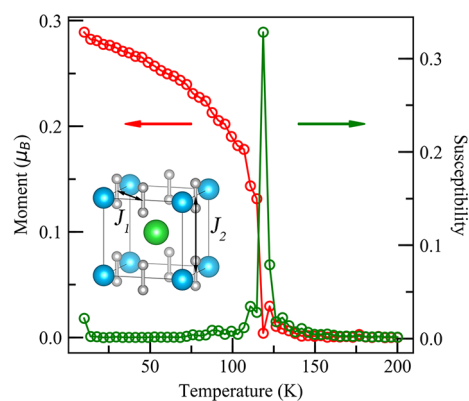
As is well known, prediction of the ground state of molecular magnetism in some compounds—in particular, in strongly electron correlated compounds—often fails if using local density approximation (LDA) and GGA as exchange correlation potentials. Using GGA+ $U$ , the magnetic ground state can be correctly reproduced if  $U$  is properly adopted,<sup>10,17,18,21,31,32</sup> here  $U$  is the electron correlation energy. RbO<sub>2</sub> is such a compound. Only when  $U$  is properly taken into account can its electronic and magnetic structures be calculated to be in good agreement with the experimental results. We follow this route and see whether this treatment can reproduce the right ground state. Our result shows that



with  $U < 4.5$  eV the ground state is FM half-metal, while with  $U \geq 4.5$  eV we got the right AFM insulating state (Figure S3, SI) without setting any constraint on symmetry, as suggested in ref 17. Therefore, using GGA+ $U$  is an effective way to determine the magnetic ground state in  $O_2$  dimer systems. Next, for  $\alpha$ -BaNaO<sub>4</sub>, we need to know: (1) whether a moment resides in each  $O_2$  dimer, (2) how these moments order in the ground state, and (3) what is the ordering temperature?

To this end, we did spin polarization calculations for  $\alpha$ -BaNaO<sub>4</sub> with a PBE functional and found that  $\alpha$ -BaNaO<sub>4</sub> is a half-metal; see Figure S4a (SI). The magnetic density, i.e., the difference between spin-up and spin-down electrons, indicates that magnetic moments of  $\alpha$ -BaNaO<sub>4</sub> originate from the  $O_2$  dimers; see Figure 3a,b. The energies for non-magnetic (NM), FM, and three other possible AFM configurations (see Figure 3c–f) are then calculated against a series of  $U$  values. Figure 3g indicates that the FM configuration is the most favored state over all others, including the NM state from  $U = 0$  to  $U = 9$  eV. These results answer questions (1) and (2). Hence,  $\alpha$ -BaNaO<sub>4</sub> is a ferromagnet in its ground state.

To answer question (3), we resort to Monte Carlo simulations based on the classical Heisenberg model. The Hamiltonian is written as  $H = \sum_{ij} J_1 M_i M_j - \sum_{kl} J_2 M_k M_l - A \sum_i (s_i^z)^2$ , where  $J_1$  and  $J_2$  are the first and second nearest-neighbor exchange coupling constants (see the inset of Figure 4), and  $A$  is the anisotropy energy parameter.  $J_1$  and  $J_1$  are



**Figure 4.** Temperature-dependent average magnetic moment and magnetic susceptibility based on Monte Carlo simulations. The inset shows an indication of exchange interaction for the nearest-neighbor  $J_1$  and next-nearest-neighbor  $J_2$ .

extracted from Figure 3g by using different energies of magnetic ordering.  $A$  is extracted from the calculations on varying spin orientations (see details in the SI). The obtained  $J_1$ ,  $J_2$ , and  $A$  are 36.9, 15.9, and 0.243 meV, respectively. Positive  $J_1$  and  $J_2$  indicate the coupling is FM. Figure 4 shows the variation of magnetic moment and magnetic susceptibility with respect to temperature. The magnetic moment decreases with increasing temperature and reaches zero at 120 K. A peak appearing at this temperature in the susceptibility indicates that  $T_c$  is about 120 K.

Like 3d and 4f metals, the local moment carried by an  $O_2$  dimer is due to the unpaired electron in each  $\pi^*$  orbital. For  $\alpha$ -BaNaO<sub>4</sub>, 0.5 electron is expected to be absent in its two  $\pi^*$  orbitals for each  $O_2$  dimer. In this case, the spins are very likely to polarize. Figure 5a,b shows the spin-resolved band structures calculated with an HSE06 hybrid functional. In the spin-up subband, a band gap of  $\sim 4$  eV separates the

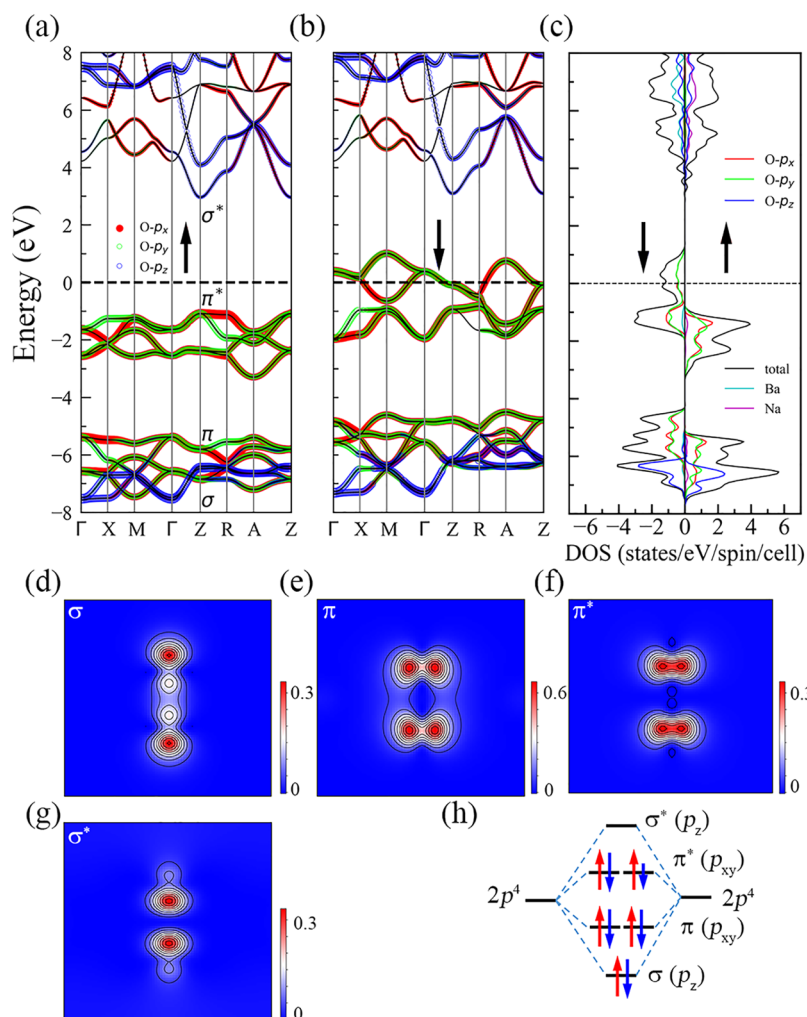
valence band, consisting of fully occupied  $\pi^*$  orbitals, and the fully empty conduction band of the  $\sigma^*$  orbital. In contrast, in the spin-down subband, the energy dispersions of unpaired electrons in the  $\pi^*$  orbitals cross the Fermi energy, resulting in a metallic feature. This is a typical half-metal. The partial density of states (Figure 5c) confirms that the states near the Fermi level predominantly come from the  $O$ -2p orbitals. The states from the Na and Ba lie far away from the Fermi level, indicating there is nearly no orbital hybridization between O and Na/Ba.  $\alpha$ -BaNaO<sub>4</sub> is essentially an ionic compound.

More specifically, the Bader charge analysis indicates that Ba loses  $1.58 e^-$ , Na loses  $0.87 e^-$ , and the  $O_2$  dimer gains  $1.23 e^-$  on average. Hence, the average valence state of  $O_2$  should be written as  $O_2^{1.5-}$ , considering the charge neutrality requirement. Figure 5d–g shows the charge density for the bands labeled in Figure 5a. Obviously, the  $p_z$ - $p_z$  orbitals of the  $O_2$  dimer form the  $\sigma$  and  $\sigma^*$  bonds, and side-to-side overlap of the  $p_x$ - $p_x$  and  $p_y$ - $p_y$  orbitals forms the  $\pi$  and  $\pi^*$  bonds. The molecular  $O_2$  feature is still preserved. Figure 5h depicts schematically the hybridization of the  $O_2$  dimer. In the spin-up subband,  $\pi^*$  bands are fully occupied by two electrons. It should be noted that, in the spin-down subband,  $\pi^*$  bands are only occupied by an average of  $1.5 e^-$ /dimer. In this way, the magnetic moment per  $O_2$  dimer should be  $0.5 \mu_B$ , consistent with the calculated magnetic moment of  $1 \mu_B$ /cell (two dimers per cell). Such an integer moment is another character of half-metals.

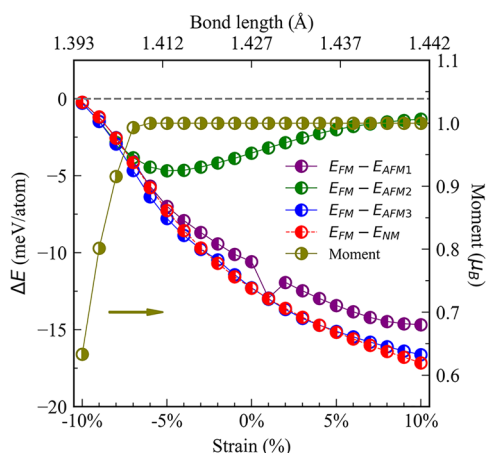
Kim et al. argued that spin–orbit coupling (SOC) along with Coulomb correlation will open a gap in the metallic channel of the FM configuration  $KO_2$ .<sup>21</sup> We examine this effect on the band structure of  $\alpha$ -BaNaO<sub>4</sub> by using GGA, GGA+ $U$ , GGA+SOC, and GGA+ $U$ +SOC as the exchange corrections. Our results found that small shifts or disappearances of degeneracy in dispersions are observed for some  $K$  points; see Figure S4. Therefore, the half-metallicity of  $\alpha$ -BaNaO<sub>4</sub> originates from partially filled  $\pi^*$  bonds, and SOC is not indispensable here.

We examine the robustness of the FM ordering under certain strains. The strain was mimicked by changing the lattice parameters,  $a$  and  $c$ , with a ratio  $\chi$ , where a negative  $\chi$  indicates compressive strain, and a positive  $\chi$  indicates tensile strain. The atomic positions are then optimized against the new parameters. As depicted in Figure 6, when compressive strain is applied, the magnetic moment remains almost unchanged within 6% strain and then rapidly decreases. The half-metallicity will disappear because the moments are less than  $1 \mu_B$ , violating the requirement of integer moment. Meanwhile, the bond length of O–O varies from 1.427 to 1.393 Å. Moreover, at a compressive strain up to 20%, the  $O_2$  dimers become much shorter,  $\sim 1.340$  Å, and non-magnetic. Similar cases are observed for SrN and SrN<sub>2</sub>, where SrN owns magnetic moments with a proper bond length for the N<sub>2</sub> dimer, while SrN<sub>2</sub> is non-spin-polarized with a shorter bond length.<sup>33</sup> So, the bond length of the  $O_2$  dimer is highly relevant to the appearance of polarized spins. After applying tensile strains within 10%, the FM holds against three AFM and NM configurations, and the half-metallic feature remains. This means that the half-metallicity is more sensitive to compressive than to tensile strains for  $\alpha$ -BaNaO<sub>4</sub>.

The ferromagnetic ordering of  $\alpha$ -BaNaO<sub>4</sub> could be explained by the coexistence of double exchange and direct exchange interactions. Its chemical formula can be written as  $Ba^{2+}Na^{+}O_2^{2-}O_2^-$ , i.e., mixed-valent  $O_2^{2-}$  and  $O_2^-$  anions



**Figure 5.** Spin and orbital resolved band structures of  $\alpha$ -BaNaO<sub>4</sub> for (a) spin-up subband and (b) spin-down subband with an HSE06 hybrid functional, where the Fermi level was set to be zero. Red circles indicate O- $p_x$  orbitals, green O- $p_y$  orbitals, and blue O- $p_z$  orbitals. The contributions of the orbitals are proportional to the size of the circle. (c) Orbital-resolved density of states contributions from Ba, Na, and O atoms in  $\alpha$ -BaNaO<sub>4</sub>. (d–g) Charge density of the (100) plane for the bands labeled in (a). (h) Schematic representation of hybridization of the  $O_2$  dimer. Note here that the extra 1.5 electrons are donated from the Ba and Na atoms.



**Figure 6.** Magnetic moment of FM configuration and energy difference between AFM1, AFM2, AFM3, and FM vary with strain. The upper axis shows the corresponding bond length of the  $O_2$  dimer at different strains.

coexist. Similar to  $La_{1-x}A_xMnO_3$  ( $A = Ca, Sr, Ba$ ), where the electron hops from  $Mn^{3+}$  to  $Mn^{4+}$  through double exchange,<sup>34</sup> the itinerant electrons in the  $\pi^*$  orbitals could hop from  $O_2^{2-}$  to  $O_2^-$  in the (001) plane mediated by  $Na^+$  ions, guaranteeing the spins are parallel.<sup>20</sup> Along the [001] direction, a positive  $J_2$  could be explained as FM interaction through direct exchange interactions among the head-to-head  $O_2$  dimers. All neighboring  $O_2$ -dimer layers are coupled ferromagnetically as expected.

$\alpha$ -BaNaO<sub>4</sub> is different from the known  $O_2$ -dimer-containing compounds in both structure and magnetic properties. First, the orientation of  $O_2$  dimers is a key factor. If they do not align in one direction, it is hard to form long-range magnetic ordering. That is the cases for  $Rb_4O_6$  and  $Cs_4O_6$ , where the  $O_2$  dimers do not align in an identical orientation, leading to frustrated magnetism.<sup>10,11</sup> Second, the coupling type between  $O_2$  dimers is important. Although the dimers align along one direction in  $AO_2$  ( $A = K, Rb, Cs$ ), they show AFM orderings because of inter-AFM coupling between adjacent planes.<sup>21</sup> In  $\alpha$ -BaNaO<sub>4</sub>, the adjacent planes couple ferromagnetically through direct interactions. The coupling switch is attributed to the difference ways  $O_2$  dimer layers stack: a shift (0.5a, 0.5a, 0) between adjacent planes for the former compounds and

head-to-head along the  $c$  direction for the latter. So, the direct-exchange interaction between adjacent  $O_2$  dimers along the  $c$ -axis plays a vital role in the formation of ferromagnetic ordering. To check this, we shift the middle layer in AFM  $RbO_2$  with a vector  $(0.5a, 0.5a, 0)$  within the unit cell, and the resultant arrangement of  $O_2$  dimers between the adjacent layers is head-to-head; see Figure S5 (SI). In this geometry, the calculated ground state changes into FM when  $U = 6.5$  eV. It should be noted that, in a tetragonal structure, the  $O_2$  dimer layers are allowed to have only these two configurations.

At low temperatures,  $AO_2$  ( $A = K, Rb, Cs$ ) usually undergo several structural transitions, where the  $O_2$  dimers would slightly incline with a small angle to lift the degeneracy of  $\pi^*$  orbitals.<sup>4,5</sup> To clarify the influence of tilted  $O_2$  dimers on the magnetic property,  $O_2$  dimers in  $\alpha$ - $BaNaO_4$  were rotated by  $30^\circ$ . As suggested in ref 21, two kinds of tilted structures were considered: type [R1], in which the  $O_2$  dimers are  $30^\circ$  off the  $z$  axis in the  $xz$  plane, see Figure S6a,b; and type [R2], in which the  $O_2$  dimers are  $30^\circ$  off the  $z$  axis in the (110) plane, see Figure S6c,d. We compared the total energies of different magnetic states. It shows the inclination of  $O_2$  dimers do not influence the ground state of  $\alpha$ - $BaNaO_4$  with  $U = 6.5$  eV or without  $U$ , see Table S2 in the SI. The FM ordering still survives.

Although other predicted structures are not energy favorable, but  $P4/nmm$ - $BaNaO$  and  $P\bar{1}$ - $BaNaO_2$  are stable in terms of lattice dynamics and mechanical dynamics, see details in the SI. We also examine their properties. They do not show spin-polarized behavior.  $P4/nmm$ - $BaNaO$  is a non-magnetic metal, and  $P\bar{1}$ - $BaNaO_2$  is a semiconductor; see Figures S7(a) and S8. It should be noted that  $P4/nmm$ - $BaNaO$ , whose chemical formula could be written as  $Ba^{2+} Na^+ O^{2-} \cdot e^-$ . The electrons were confined between the empty space formed by  $Na^+$  ions; see Figure S7b. It may be a potential electrified material,<sup>35</sup> which deserves further investigation.

We note that  $N_2$  dimers can also induce magnetism in some nitrides if there exist unpaired electrons in its  $\pi^*$  orbitals, such as  $SrN$ .<sup>33</sup> Besides,  $N_2$  dimers were predicted to form other nitrides with main group element and  $3d$  metals, which can be a metal with excellent thermal and electrical conductivity for  $SiN_4$ <sup>36</sup> and a half-metal for  $FeN_4$ .<sup>37</sup> More novel magnetic and other emergent properties are expected in these compounds containing  $O_2$  and  $N_2$  dimers.<sup>38</sup> Hayyan and co-workers recently gave a very comprehensive review on the generation and implications of  $O_2^-$ .<sup>39</sup> This will be helpful in synthesizing the molecule oxygen containing compounds, including these ternary ones.

## CONCLUSION

In summary, by first-principles calculations, we show that  $\alpha$ - $BaNaO_4$  is a half-metal. It is energetically favorable, and its lattice is dynamically, mechanically, and thermally stable. It possesses robust FM ordering with a  $T_c$  of 120 K. The partially occupied  $\pi^*$  orbitals in the metallic channel and fully occupied  $\pi^*$  orbitals in the semiconducting channel is the origin of half-metallicity. Unlike previously reported  $AO_2$  ( $A = K, Rb, Cs$ ) with AFM orderings between (001) layers through indirect exchange interactions, the  $O_2$  dimer layers in  $\alpha$ - $BaNaO_4$  coupled ferromagnetically to each other through direct interactions, with head-to-head alignment along the [001] direction. Our work provides new insights in exploring the FM and half-metallicity in  $O_2$ -dimer-containing compounds.

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/jacs.9b13295>.

Lattice parameters; elastic constants; details of estimation coupling constant; phonon spectra and band structures of  $BaNaO_x$ ; molecular dynamics simulations of  $BaNaO_4$ ; more band structure results of  $BaNaO_4$ ; shifted configuration of  $RbO_2$ ; structures and formation enthalpies of related compounds (PDF)

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### Notes

The authors declare no competing financial interest.

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