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Picotesla-sensitivity microcavity optomechanical magnetometry

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Abstract

Cavity optomechanical systems have enabled precision sensing of magnetic fields, by leveraging the optical resonance-enhanced readout and mechanical resonance-enhanced response. Previous studies have successfully achieved mass-produced and reproducible microcavity optomechanical magnetometry (MCOM) by incorporating Terfenol-D thin films into high-quality (Q) factor whispering gallery mode (WGM) microcavities. However, the sensitivity was limited to $585 \text{ pT Hz}^{-1/2}$, over 20 times inferior to those using Terfenol-D particles. In this work, we propose and demonstrate a high-sensitivity and mass-produced MCOM approach by sputtering a FeGaB thin film onto a high- Q SiO_2 WGM microdisk. Theoretical studies are conducted to explore the magnetic actuation constant and noise-limited sensitivity by varying the parameters of the FeGaB film and SiO_2 microdisk. Multiple magnetometers with different radii are fabricated and characterized. By utilizing a microdisk with a radius of $355 \mu\text{m}$ and a thickness of $1 \mu\text{m}$, along with a FeGaB film with a radius of $330 \mu\text{m}$ and a thickness of $1.3 \mu\text{m}$, we have achieved a remarkable peak sensitivity of $1.68 \text{ pT Hz}^{-1/2}$ at 9.52 MHz . This represents a significant improvement of over two orders of magnitude compared with previous studies employing sputtered Terfenol-D film. Notably, the magnetometer operates without a bias magnetic field, thanks to the remarkable soft magnetic properties of the FeGaB film. Furthermore, as a proof of concept, we have demonstrated the real-time measurement of a pulsed magnetic field simulating the corona current in a high-voltage transmission line using our developed magnetometer. These high-sensitivity magnetometers hold great potential for various applications, such as magnetic induction tomography and corona current monitoring.

Introduction

High-sensitivity magnetometers play a crucial role in both fundamental research and practical applications, including spin physics in condensed matter systems¹, dark matter detection², nuclear magnetic resonance³, magnetocardiography⁴, magnetoencephalography⁵, mineral exploration⁶, nondestructive inspection⁷, magnetic induction tomography^{8,9}, and current detection^{10–14}. Currently, the state-of-the-art magnetometers are based on superconducting quantum interference devices

(SQUIDs), with exceptional sensitivity at the $\text{fT Hz}^{-1/2}$ level¹⁵. However, their reliance on cryogenic systems has resulted in elevated operational costs and limited applications. Recently, various magnetometers that can work at room temperature have been developed, such as atomic magnetometers¹⁶, diamond nitrogen-vacancy color center magnetometers¹⁷, and magnetostrictive material magnetometers¹⁸. In the past few years, high-quality (Q) factor whispering gallery mode (WGM) optical microcavities have been widely explored for various applications due to the enhanced light-matter interactions, including quantum optics^{19,20}, integrated photonic network²¹, optical filters²², optical frequency combs²³, and highly-sensitivity sensing^{24–29}. Microcavity optomechanical magnetometry (MCOM)^{30–38} has recently been developed by incorporating magnetostrictive materials into high- Q WGM

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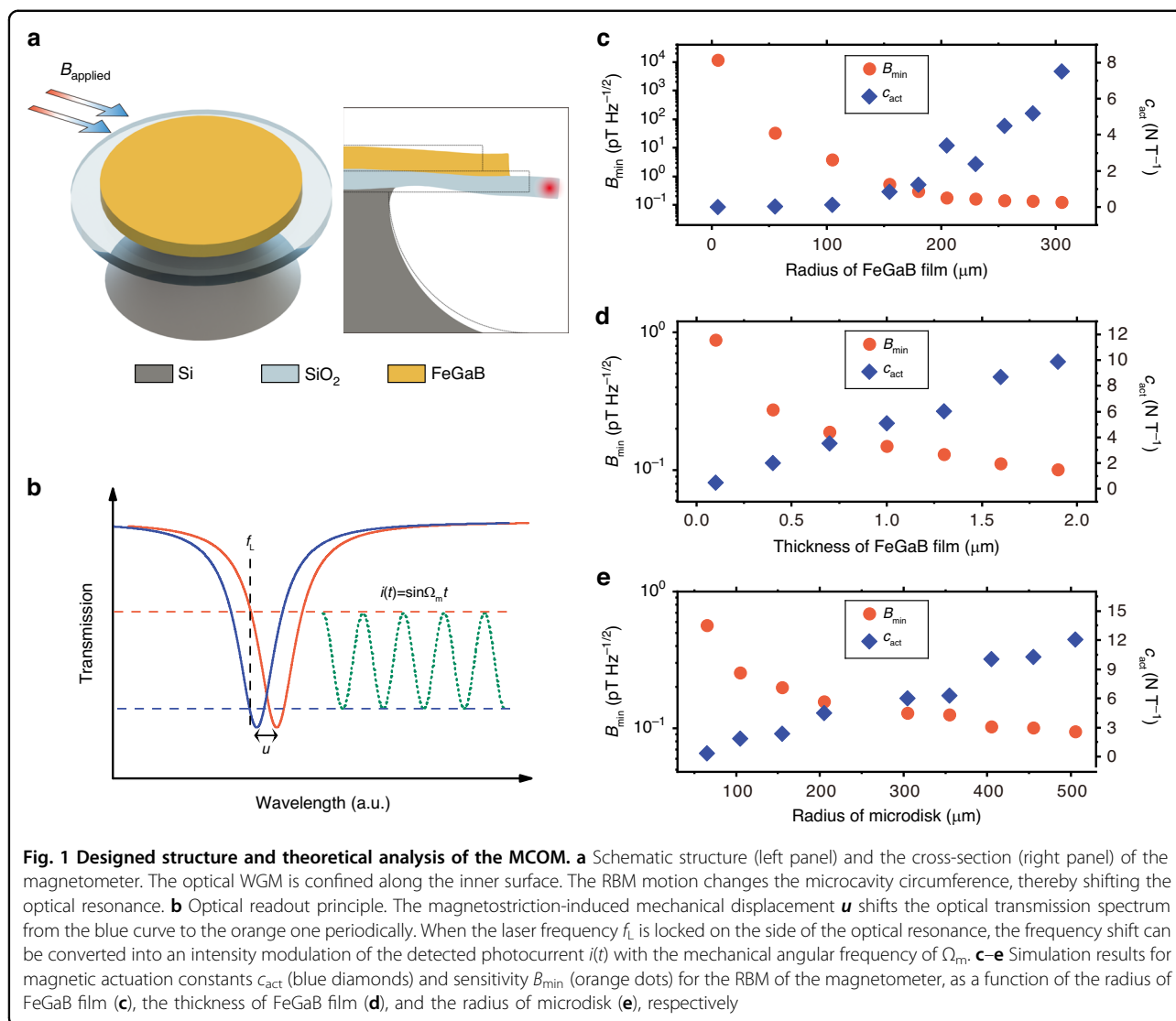
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optical microcavities, which offer advantages of miniaturization and low power consumption; ease of on-chip integration; high sensitivity and broad bandwidth. In these magnetometers, the magnetic field induces strain in the magnetostrictive material, which can drive the mechanical motion of the microcavity and result in a change in the radius of the microcavity (Fig. 1a). This radius change shifts the optical resonance, resulting in a periodic change in the intracavity field (Fig. 1b). Consequently, the magnetic field can be optically read out, with its sensitivity enhanced by both the optical and mechanical resonances. Furthermore, cavity optomechanical systems have enabled precision sensing of various physical quantities, including displacement³⁹, mass⁴⁰, force⁴¹, acceleration^{42,43}, and ultrasound waves^{44–47}, etc.

The first MCOM was realized by manually depositing a particle of magnetostrictive material, Terfenol-D, on the top of a microcavity and bonding it using epoxy³⁰.

However, its sensitivity was limited to a few hundreds of $\text{nT Hz}^{-1/2}$ due to the small overlap between the magnetostrictive force and the mechanical mode of the microcavity. The sensitivity was then improved by depositing the Terfenol-D particle into the central hole of the microcavity^{31,33,34}, achieving a peak sensitivity of $26 \text{ pT Hz}^{-1/2}$ at 10.5 MHz ³⁴. Resonant magnon-assisted optomechanical magnetometers have recently been realized, achieving a peak sensitivity of $850 \text{ pT Hz}^{-1/2}$ at a frequency of 206 MHz ³⁶. These magnetometers working at the MHz frequency band have various potential applications, such as corona current monitoring in high-voltage transmission line systems¹³, magnetic induction tomography^{8,9}, and nuclear magnetic resonance in the human body³. However, the fabrications of these magnetometers involving manual deposition of magnetostrictive materials are intricate, posing significant challenges for mass-production and reproducible

fabrication. A more mass-produced and reproducible fabrication method was developed by sputtering coating Terfenol-D thin films into SiO₂ microtoroids³⁷. Nevertheless, the achieved peak sensitivity of 585 pT Hz^{-1/2} is more than one order of magnitude inferior to that achieved in magnetometers using Terfenol-D particles³⁴. Additionally, the vulnerability to oxidation of Terfenol-D further limits their applications.

In this work, we have successfully developed mass-produced and high-sensitivity MCOM by sputter coating thin films of a new magnetostrictive material, FeGaB, onto high-Q microdisk cavities. We derive the expression of sensitivity of the MCOM using the intensity modulation mechanism and study how various parameters affect the sensitivity. We have made several key improvements experimentally to enhance the device performance compared to previous works. Firstly, we replace the magnetostrictive material Terfenol-D with FeGaB, as FeGaB exhibits superior soft magnetic properties, including lower coercivity, lower saturation magnetic field, and a larger maximum piezomagnetic coefficient^{48–50}. Secondly, we conduct comprehensive simulations to explore the relationship between the sensitivity and the geometric parameters of the FeGaB films and SiO₂ microdisks. Subsequently, we fabricate magnetometers with varying microdisk radii. Thirdly, we optimize the optical frequency detuning between the incident laser and the optical mode, minimizing the contribution of the shot noise to the total noise. Lastly, microdisk cavities are used in this work, offering improved reproducibility compared with microtoroids used in earlier studies³⁷. Remarkably, we achieve a peak sensitivity of 1.68 pT Hz^{-1/2} at 9.52 MHz using a magnetometer with a SiO₂ microdisk radius of 355 μm and a thickness of 1 μm, along with a FeGaB film radius of 330 μm and a thickness of 1.3 μm. This sensitivity surpasses previous mass-produced MCOM by over two orders of magnitude. Furthermore, we explore a proof-of-concept application by detecting a pulsed magnetic field signal, simulating corona current detection in high-voltage transmission lines. These findings demonstrate the potential of our fabricated high-sensitivity magnetometers for various practical applications, such as magnetic induction tomography and corona current detection.

Results

Theoretical analysis

Figure 1a presents a schematic structure of our designed MCOM. It consists of a SiO₂ microdisk with a thin FeGaB film deposited on top, supported by a silicon pedestal. The magnetometer supports both high-Q optical and mechanical modes, as illustrated in the right panel of Fig. 1a. When a magnetic field is applied, the magnetostriction of the FeGaB film can drive the mechanical displacement (u)

of the microcavity, which modifies the circumference of the microcavity and therefore shifts the optical resonance, as illustrated in Fig. 1b. The magnetic field amplitude can thus be converted into the amplitude or phase modulation of the intracavity field, which can be optically read out from the detected photocurrent $i(t)$.

We first conduct a thorough theoretical analysis of the sensitivity of our MCOM. To read out the magnetic field, we employ a technique where the laser frequency is locked on the side of the optical resonance using thermal locking⁵¹. This allows for a straightforward implementation of the intensity modulation readout mechanism (as shown in Fig. 1b), which is commonly used in optomechanical sensing experiments^{34,38,44,45}. In the case of the intensity modulation readout mechanism, it is necessary to consider the detuning between the laser frequency ω_L and the cavity resonance frequency ω_o : $\Delta = \omega_L - \omega_o$. However, previous studies have determined the power spectral densities of displacement noise under the assumption of zero frequency detuning^{52–54}. Hence, we take this detuning into account and obtain the sensitivity of the magnetometers using the intensity modulation readout mechanism under any coupling condition. Here, we define $\kappa_0 = \eta\kappa_1$, where $\eta > 1$, $\eta = 1$, $\eta < 1$ denoting the under-coupled, critical-coupled, and over-coupled conditions, respectively (see Section 1 in the Supplementary Information). The sensitivity of the magnetometer, $B_{\min}(\Omega)$, defined as the minimum detectable magnetic field at different frequencies with a measurement resolution bandwidth (RBW) of 1 Hz, can be expressed as:

$$\begin{aligned} B_{\min}(\Omega) &= \frac{1}{c_{\text{act}}} \sqrt{\left(\frac{S_{\text{thermal}}}{A_1 |\chi_{\Delta}|^2} + \frac{S_{\text{shot}}}{A_1 |\chi_{\Delta}|^2} + \frac{S_{\text{back-action}}}{A_1 |\chi_{\Delta}|^2} \right) \cdot 2p_{\text{zp}}^2} \\ &= \frac{1}{c_{\text{act}}} \sqrt{2m_{\text{eff}} \gamma k_B T + \frac{P_{\text{zp}}^2}{A_1 |\chi_{\Delta}|^2} + 2A_2 m_{\text{eff}} \gamma \hbar \Omega_m |C_{\text{eff}}^{\Delta}|} \end{aligned} \quad (1)$$

Here, Ω is the Fourier frequency, $A_1 = \frac{4g^2 \kappa_1 |\Delta^2 \cos^2 \theta + (\frac{\eta+1}{4} \kappa_1^2 + \Omega^2) \sin^2 \theta - \frac{\eta+1}{2} \kappa_1 \Delta \sin 2\theta|}{(\frac{\eta+1}{4} \kappa_1^2 - \Omega^2 + \Delta^2)^2 + (\eta+1)^2 \kappa_1^2 \Omega^2}$, $A_2 = \frac{(\frac{\eta+1}{4} \kappa_1^2 + \Omega^2) (\Delta^2 + \frac{\eta+1}{4} \kappa_1^2 + \Omega^2)}{(\frac{\eta+1}{4} \kappa_1^2 - \Omega^2 + \Delta^2)^2 + (\eta+1)^2 \kappa_1^2 \Omega^2}$, are constants associated with the coupling condition η and frequency detuning Δ . Here, κ_1 represents the external energy decay rate of the optical mode and $\theta = \arctan\left(\frac{\text{Im}(\alpha_{\text{out}})}{\text{Re}(\alpha_{\text{out}})}\right)$ denotes the phase angle of the output field. $\text{Re}(\alpha_{\text{out}})$ and $\text{Im}(\alpha_{\text{out}})$ denote the real and imaginary parts of the cavity field, respectively. $g = g_0 \sqrt{N}$ is the cavity-enhanced optomechanical coupling rate, where g_0 is the single-photon optomechanical coupling rate defined as $g_0 = G_{\text{om}} x_{\text{zpp}}$. Here, $G_{\text{om}} = \frac{d\omega_o}{dR}$ is the optomechanical coupling coefficient, which quantifies how much ω_o shifts with the radius (R) change. x_{zpp} denotes the zero-point displacement of the mechanical mode. N represents the

steady-state photon number in the cavity. m_{eff} is the effective mass of the mechanical mode. γ is the energy decay rate of the mechanical mode. k_B is the Boltzmann constant, T is the temperature. Ω_m is the angular frequency of the mechanical mode. $C_{\text{eff}}^{\Delta}(\Omega) = \frac{4g^2}{\kappa\gamma(1-2i\Omega/\kappa)^2}$ is effective optomechanical cooperativity. $\chi_{\Delta}(\Omega) =$

$\frac{\Omega_m}{-\Omega^2 - i\Omega\gamma + \Omega_m^2 + \frac{4g^2\Omega_m\Delta}{(\kappa/2 - i\Omega)^2 + \Delta^2}}$ is the modified mechanical suscept-

ibility in the presence of the optical field. $p_{\text{zp}} = \sqrt{\frac{\hbar m_{\text{eff}} \Omega_m}{2}}$ denotes the zero-point-fluctuation momentum. $c_{\text{act}} = F/B$ is the magnetic actuation constant, which characterizes how well the magnetic field is converted into an applied force on the mechanical resonator³⁰.

According to Eq. (1), the sensitivity is determined by the sensor noise and the value of c_{act} . The sensor noise is represented by the formula inside the square root, with the three terms representing thermal noise, shot noise, and back-action noise, respectively. The back-action noise is typically much smaller than the thermal noise and therefore is negligible (see Fig. S1 in the Supplementary Information). In comparison to previous studies conducted under the condition of zero frequency detuning^{53,54}, the thermal-noise-dominant sensitivity remains unchanged, which is determined by T , m_{eff} , and γ . Conversely, the shot noise-dominant sensitivity is modified and is dependent on the detuning Δ . When the laser is blue-detuned ($\Delta > 0$), γ is reduced, which is beneficial for magnetic field sensing. Conversely, when the laser is red-detuned ($\Delta < 0$), γ is increased, which can deteriorate the sensitivity. Additionally, the value of Δ also affects A_1 . To quantify the contribution of the shot noise to the total noise, we investigate the ratio of total noise to shot noise ($S_{\text{total}}/S_{\text{shot}}$) as a function of the transmission T which is determined by the laser detuning Δ . It is found that $S_{\text{total}}/S_{\text{shot}}$ reaches its maximum when $T = 1/4$ for the critical-coupled condition ($\eta = 1$) with the minimum transmission being 0, as shown in Fig. S1c. For more general cases ($\eta \neq 1$), $S_{\text{total}}/S_{\text{shot}}$ reaches its maximum when $T = \frac{1}{4} \times (1 - T_{\text{min}}) + T_{\text{min}}$, with T_{min} denoting the value of the minimum transmission. For more details, see Section 1 of the Supplementary Information. Consequently, in our following experiment of magnetic field sensing, we lock the laser frequency on the blue side of the optical mode and keep the transmission at 1/4. It can also be seen that the value of κ_1 also affects A_1 . We study the relationship between sensitivity and intrinsic optical quality factor Q_o under the critical-coupled condition ($\eta = 1$) in Section 2 of the Supplementary Information. The sensitivity of the magnetometer increases linearly with the increase of Q_o . This linear trend reaches a plateau when Q_o exceeds a transition point, where the sensitivity of the magnetometer is optimal. For details, see Section 2 in the Supplementary Information.

To enhance the magnetic field sensitivity, it is crucial to optimize c_{act} to be as high as possible. Specifically, the expression of c_{act} in the frequency domain can be expressed as⁵⁵:

$$c_{\text{act}}(\Omega) = \frac{F_{\text{signal}}(\Omega)}{B_{\text{applied}}(\Omega)} = \frac{\max[\mathbf{u}(\Omega)]m_{\text{eff}}\Omega_m}{\chi(\Omega)B_{\text{applied}}(\Omega)} \quad (2)$$

Here, $\chi = \frac{\Omega_m}{-\Omega^2 - i\Omega\gamma + \Omega_m^2}$ is the mechanical susceptibility, and $\max[\mathbf{u}(\Omega)]$ is the maximum displacement of the mechanical mode induced by an applied magnetic field, obtained using the finite element method (FEM) simulation. The value of $c_{\text{act}}(\Omega)$ depends on the geometric parameters of the magnetometer and the piezomagnetic coefficient of the magnetostrictive film. Therefore, we simulate $c_{\text{act}}(\Omega)$ and $B_{\text{min}}(\Omega_m)$ with different geometric parameters using the method proposed in ref.⁵⁵. Specifically, we optimize the parameters for the RBM, since its motion is primarily radial, which aligns well with the direction of magnetostriction. Furthermore, the RBM exhibits the highest optomechanical coupling coefficient G_{om} , resulting in the highest optical transduction sensitivity. It can also be found that c_{act} increases linearly with the piezomagnetic coefficient.

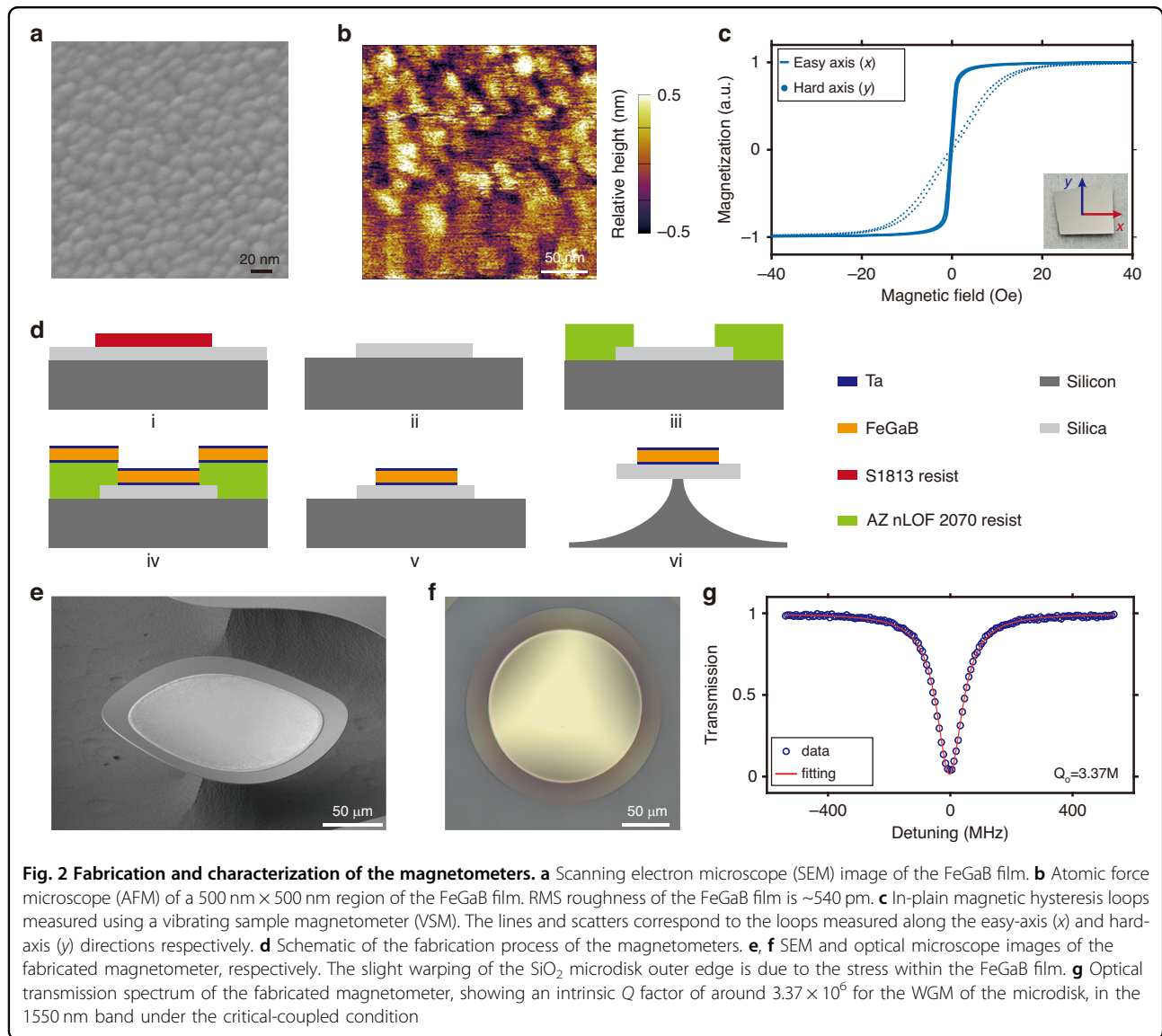
Figure 1c illustrates the relationship between c_{act} ($B_{\text{min}}(\Omega_m)$) and the radius of the FeGaB film. In these simulations, we keep the radius of the microdisk at 305 μm and the radius of the silicon pedestal at 106 μm , which are consistent with our experimental parameters. When the radius of the FeGaB film is smaller than that of the silicon pedestal, the deformation induced by the magnetostriction effect of the film is constrained by the pedestal, leading to a relatively small value of c_{act} . As the radius of the FeGaB film exceeds that of the silicon pedestal, the mechanical modes can be effectively actuated by the magnetostrictive force, resulting in a larger c_{act} . Therefore, a larger radius of FeGaB film indicates a better magnetic field sensitivity. Taking into account the absorption of optical field energy by FeGaB material and the alignment precision in the fabrication process, we set the radius of the FeGaB film to be 25 μm smaller than that of the microdisk. In Fig. 1d, we study the effect of the thickness of FeGaB film on c_{act} and $B_{\text{min}}(\Omega_m)$, where the radii of the microdisk and FeGaB film are set as 305 μm and 280 μm , respectively. The results suggest that thicker FeGaB films yield better sensitivity and magnetic actuation constants. However, as the thickness increases, there is a higher risk of the FeGaB film peeling off from the microdisk. As a compromise, we utilize a thickness of 1.3 μm for the FeGaB film in the fabrication of our magnetometers. In Fig. 1e, we vary the radius of the microdisk from 65 μm to 505 μm , while keeping the radius of FeGaB film 25 μm smaller than that of the microdisk. It shows that the theoretical sensitivity for each

radius maintains below $1 \text{ pT Hz}^{-1/2}$, with a slight improvement as the radius of the microdisk increases. This result shows that by adjusting the microdisk radius, we can achieve highly sensitive detection of magnetic fields across a wide frequency range in the megahertz bands.

Device fabrication and characterization

To characterize the properties of the magnetostrictive material, we start by sputter coating the FeGaB film onto a $1 \text{ cm} \times 1 \text{ cm}$ blank silica substrate with the deposition details shown in the “Materials and methods” section. Figure 2a presents a scanning electron microscope (SEM) image of the deposited Ta/FeGaB/Ta stack film. This suggests that the incorporation of boron atoms into the FeGa alloys results in a refined grain size⁴⁹. Figure 2b

presents the two-dimensional surface tomography obtained with atomic force microscope (AFM). The root-mean-square (RMS) roughness of this film is determined to be approximately 540 pm. The magnetization of the FeGaB film is measured using a vibrating sample magnetometer (VSM, Lake Shore 7404). To determine the saturation magnetization and assess the magnetic anisotropy of the films, in-plane hysteresis loops are recorded with field parallel and perpendicular to the field applied during the deposition process, denoted as x and y in the inset of Fig. 2c. Figure 2c displays the hysteresis loops of the deposited FeGaB film in both the easy-axis (x) and hard-axis (y) directions, represented in the solid curve and dots, respectively. The FeGaB film exhibits an anisotropy field of approximately 20 Oe and a coercivity of around 0.4 Oe. The saturation magnetization is calculated to be



around $1.08\text{--}1.23 \times 10^3 \text{ emu cm}^{-3}$, which is consistent with the values reported in ref.⁴⁹. Notably, our deposited FeGaB film has significantly improved soft magnetic properties compared with Terfenol-D, which has an anisotropy field of 1000 Oe and a coercivity of approximately 6 Oe^{56,57}. Additionally, although the saturation magnetostriction coefficient of Terfenol-D (~ 2000 ppm) is significantly larger than that of FeGaB (~ 70 ppm), the maximum piezomagnetic coefficient of FeGaB ($\sim 6 \text{ ppm Oe}^{-1}$) is higher than that of Terfenol-D ($\sim 2.6 \text{ ppm Oe}^{-1}$)^{48,50}. These parameters indicate that FeGaB is more sensitive to small magnetic fields compared with Terfenol-D.

Figure 2d illustrates the fabrication process of our designed magnetometers, with the fabrication details shown in the “Materials and methods” section. Figure 2e, f display the SEM and optical microscope images of the fabricated magnetometers with a microdisk radius of 105 μm , respectively. The slight warping observed in the SiO₂ microdisk is attributed to the stress within the FeGaB film, which is measured to be approximately 260 MPa. Figure 2g presents the optical transmission spectrum of the microdisk, showing an intrinsic optical Q_o factor of 3.37×10^6 under the critical-coupled condition.

Sensitivity

The sensitivity of our magnetometers is characterized using the setup depicted in Fig. 3a. A tunable laser in the 1550 nm band is utilized to evanescently couple light into the WGM of the microdisk via a tapered fiber. The polarization of the light is optimized using a fiber polarization controller to match the polarization of the WGM. The transmitted light from the tapered fiber is collected by a photodetector (PD) and subsequently measured using an oscilloscope (OSC), electronic spectrum analyzer (ESA), and vector network analyzer (VNA), respectively. The transmission spectrum of the microdisk is recorded using the OSC as the laser wavelength is scanned. A coil positioned 3 mm away from the magnetometer is driven by an AFG or VNA, to generate a magnetic field along the hard-axis direction of the FeGaB film. The magnetic field within the frequency range of 0–50 MHz is calibrated using a commercial Gaussmeter and the VNA. The wavelength of the laser is thermally locked on the blue-detuned side of the high-Q optical mode. The mechanical motion induced by the applied magnetic field modulates the radius of the microdisk, thereby altering its optical resonance. This is converted into a periodic modulation in the intensity of the transmitted light. To optimize the readout sensitivity, the laser frequency detuning is set as $\Delta = \frac{\kappa}{2\sqrt{3}}$ under the critical-coupled condition, corresponding to a transmission of $T = 1/4$. The noise power spectrum of the mechanical mode is measured by the ESA. Additionally, the magnetic

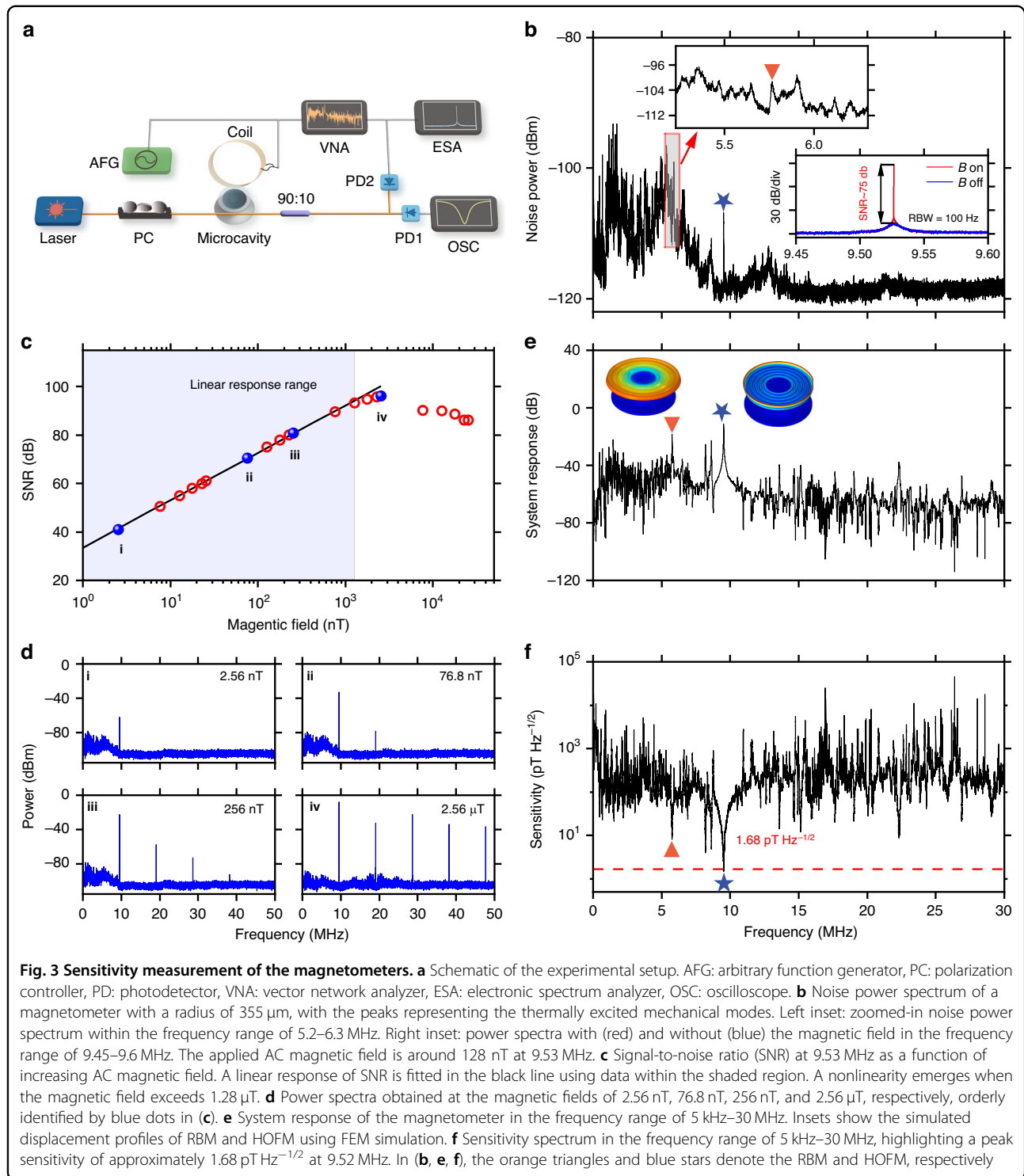
response of the magnetometer at different frequencies can be obtained by sweeping the frequency using the VNA.

Figure 3b shows the measured noise power spectrum $S(\Omega)$ in the frequency range of 5 kHz–30 MHz of a magnetometer with a microdisk radius of 355 μm . The multiple characteristic peaks correspond to thermally excited mechanical modes. The left inset in Fig. 3b presents the zoomed-in noise power spectrum around the RBM. By applying a magnetic field of around 128 nT at the frequency of $\Omega_{\text{ref}}/2\pi = 9.53$ MHz, a signal peak above the thermal noise is obtained, exhibiting a signal-to-noise ratio (SNR) of 75 dB, as shown in the right inset of Fig. 3b. To validate that the applied magnetic field of 128 nT falls within the linear response range of the magnetometer, we investigate the SNR at 9.53 MHz, under increasing the magnetic field ranging from 2.56 nT to 25.6 μT . Figure 3c presents the SNR at 9.53 MHz for different magnetic fields, demonstrating a linear response range of 2.56 nT–1.28 μT , with its linear fitting shown in the black line using data within the shaded region. Consequently, the sensitivity at 9.53 MHz can be obtained from the following equation³⁰:

$$B_{\min}(\Omega_{\text{ref}}) = \frac{|B_{\text{applied}}(\Omega_{\text{ref}})|}{\sqrt{\text{SNR}(\Omega_{\text{ref}})\Delta\Omega_{\text{RBW}}}} \quad (3)$$

Here, $B_{\text{applied}}(\Omega_{\text{ref}})$ represents the applied magnetic field at 9.53 MHz and $\Delta\Omega_{\text{RBW}} = 2\pi \times 100$ Hz is the RBW of the ESA. The sensitivity at 9.53 MHz can be calculated as 2.28 pT Hz^{-1/2}. As the AC magnetic field exceeds 1.28 μT , a noticeable nonlinearity in the response emerges. Figure 3d presents the power spectra in the range of 5 kHz–50 MHz at four different magnetic fields marked by blue dots in Fig. 3c. It is shown that with the increase of the magnetic field, higher-order mechanical sidebands arise due to the nonlinear transduction. Since the cavity mode is a Lorentzian lineshape, the optical readout signal for displacement is a harmonic oscillation only for a small displacement⁴⁴. After the saturation of the first-order sideband, the dynamic range can be effectively expanded by detecting SNRs of the higher-order mechanical sidebands⁵⁸. Additionally, a decline of SNR is observed as the applied magnetic field increases to 7.68 μT . This decline can be attributed to the reduction in intracavity power when the mechanical displacement induced by the magnetic field is very large^{59–61}. In the case of large displacement, cascaded n photon-phonon scattering events occur. This leads to a large fraction of the intracavity photons being scattered, resulting in additional transmission dips near each detuning $\Delta = n\Omega_{\text{m}}$. The transmission spectra at different magnetic fields are presented in Section 4 in the Supplementary Information.

The measured system response $N(\Omega)$ in the frequency range of 5 kHz–30 MHz is presented in Fig. 3e. The orange triangle and blue star represent the RBM at



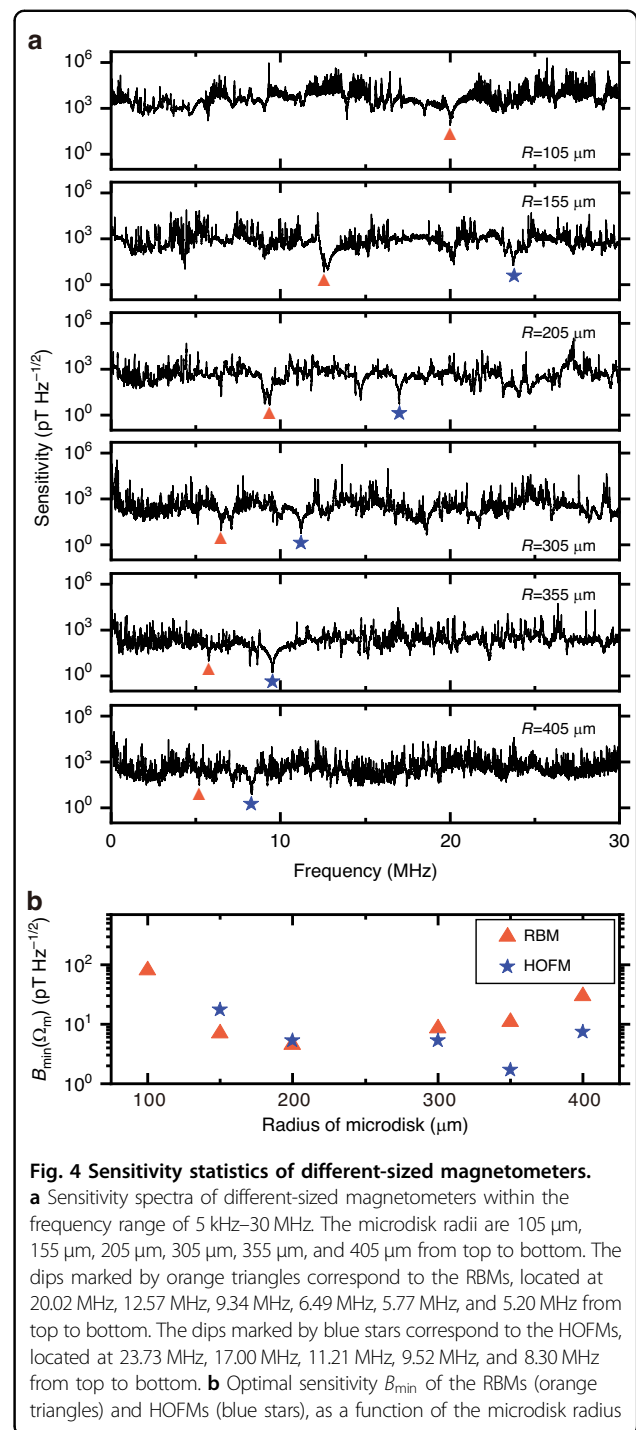
5.76 MHz and the high-order flapping mode (HOFM) at 9.53 MHz, whose displacement profiles are shown in the insets, obtained by FEM simulation. As shown in Fig. 3f, we calculate the sensitivity in a broad frequency range, by

using the equation^{30,44}:

$$B_{\min}(\Omega) = B_{\min}(\Omega_{\text{ref}}) \frac{B_{\text{applied}}(\Omega)}{B_{\text{applied}}(\Omega_{\text{ref}})} \sqrt{\frac{N(\Omega)}{N(\Omega_{\text{ref}})} \cdot \frac{S(\Omega_{\text{ref}})}{S(\Omega)}} \quad (4)$$

The orange triangle and blue star in Fig. 3f correspond to the RBM and HOFM modes indicated in the insets of Fig. 3e. In Eq. (4), $S(\Omega)$ is the noise power spectrum obtained without any applied magnetic field, as shown in Fig. 3b. $B_{\text{applied}}(\Omega_{\text{ref}})$ denotes the amplitude of the applied magnetic field within the frequency range. Note that the amplitude of the magnetic field varies with frequency when the amplitude of the driving voltage is the same, due to the impedance change of the coil at different frequencies caused by inductance. The peak sensitivity of $1.68 \text{ pT Hz}^{-1/2}$ is achieved at a frequency of 9.52 MHz , consistent with the theoretical sensitivity of $1.5 \text{ pT Hz}^{-1/2}$. The 3 dB bandwidth around this frequency is about 60 kHz , which is related to the optical quality factor, the incident laser power, the optical detuning, and the mechanical quality factor. For details, see Section 3 in Supplementary Information. However, the sensitivity of the RBM at 5.76 MHz is $9.18 \text{ pT Hz}^{-1/2}$, which is significantly lower than the theoretical prediction of $126 \text{ fT Hz}^{-1/2}$. The discrepancy in B_{min} for the RBM may be ascribed to the coupling between the RBM and other mechanical modes. As illustrated in the left inset of Fig. 3b, the power spectrum of the RBM overlaps significantly with that of other mechanical modes, indicating that magnetic fields may simultaneously drive multiple mechanical modes around the RBM, thereby weakening the drive to the RBM. Notably, the achieved sensitivity is more than two orders of magnitude improvement compared with previous mass-produced and reproducible magnetometers³⁷. Even when compared with the magnetometers that used Terfenol-D particles³⁴, our device still demonstrates a factor of 15 times sensitivity enhancement.

To investigate the relationship between the sensitivity of the magnetometers and the microdisk radius, we fabricate magnetometers with various radii. Figure 4a presents typical sensitivity spectra of six magnetometers with radii of $105 \mu\text{m}$, $155 \mu\text{m}$, $205 \mu\text{m}$, $305 \mu\text{m}$, $355 \mu\text{m}$, and $405 \mu\text{m}$, respectively, within the frequency range of 5 kHz – 30 MHz . The magnetic response of the magnetometer can be significantly enhanced by the mechanical resonances of microdisks, resulting in numerous dips at mechanical resonance frequencies throughout the magnetic sensitivity spectra. The dips marked by orange triangles and blue stars represent the RBMs and HOFMs, respectively. The HOFM of the magnetometer with the microdisk radius of $105 \mu\text{m}$ is not marked because its mode frequency exceeds 30 MHz . It is observed that the frequencies of both mechanical modes decrease as the radius of the microdisk increases. Figure 4b illustrates the optimal sensitivity B_{min} of the RBM and HOFM for microdisks with different radii. For the RBM, the optimal sensitivity improves as the radius of the microdisk increases from $105 \mu\text{m}$ to $205 \mu\text{m}$, which is consistent



with the theoretical results in Fig. 1e. However, this trend deviates from the theory for microdisks with radii of $305 \mu\text{m}$ to $405 \mu\text{m}$. In Fig. 1e, when calculating the trend of sensitivity with the radius of the microcavity, we set the mechanical quality factor to be the same for microcavities with different radii. In the experiment, we find that for cavities with relatively small radii, the supporting silicon pedestal can be etched thin enough such that the

clamping loss of the mechanical mode is small, and the mechanical quality factor is large. However, for those with relatively large radii, the stress-induced buckling and even cracking of the disks prevent us from etching the pedestals with very thin diameters. The relatively thick silicon pedestals increase the clamping loss and thus decrease the mechanical quality factors of the microdisks. This may result in a deviation between the experimental sensitivity and the theoretical calculations for larger microdisks. A similar trend of optimal sensitivity is also observed for the HOFM.

Corona current detection

High-voltage direct current (HVDC) transmission lines play an essential role in long-distance power transmission. When the high voltage is applied, the intense electric field exits near the conductor's surface. Once the electric field exceeds the threshold of air ionization, self-sustaining corona discharge occurs in the surrounding air, which results in energy loss along with audible noise, release of ozone gas, and radio interference. To mitigate these effects, one can improve the design of the HVDC transmission lines, by analyzing the characteristics of the corona current induced by the discharge. The corona current has rich frequency components typically within the range of 0–100 MHz¹³. Consequently, detecting corona current requires sensors with high sensitivity and broad bandwidth. In recent years, several photoelectric-based methods for corona current measurement have been proposed. Most of these methods involve placing resistors in series with the transmission line to record the electric current signals, which are then read out using photodiodes^{13,62}. In this work, we demonstrate corona current measurement using our magnetometers, by detecting the weak magnetic field generated by the corona current outside the transmission line, as illustrated in Fig. 5a. Compared with the previously reported photoelectric-based method, the MCOM provides a nondestructive and all-optical measurement method. It has the advantage of reduced insulation requirement and immunity to electromagnetic interference.

In our proof-of-concept application, we simulate the corona current on a 500 kV transmission line using an AFG to generate a pulsed voltage signal, as shown in Fig. 5b. This pulsed voltage signal is applied to the coil to generate a pulsed magnetic field, that can be measured using our magnetometer. The repetition frequency is 2.5 MHz, and the peak amplitude is 2.822 V, corresponding to a peak amplitude of 31.695 mA in the coil^{13,63}. This current generates a pulsed magnetic field with a peak amplitude of 11.4 μ T at the position of the magnetometer. The red curve in Fig. 5c shows the time-domain response of the magnetometer to the pulsed current signal, with a microdisk radius of 205 μ m, while

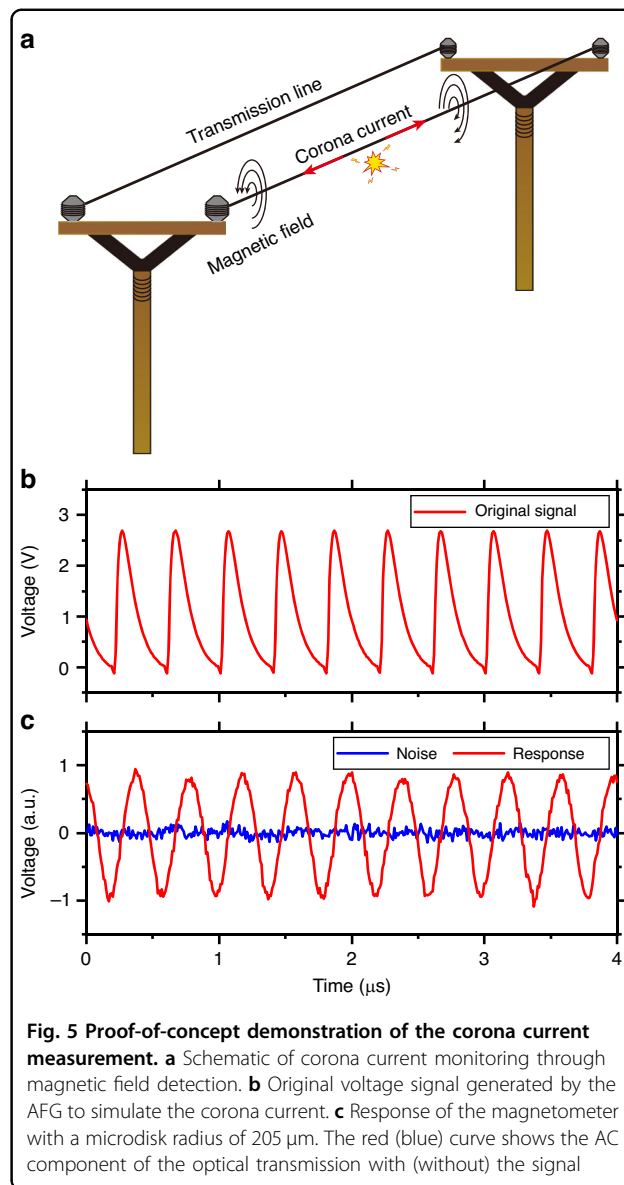


Fig. 5 Proof-of-concept demonstration of the corona current measurement. **a** Schematic of corona current monitoring through magnetic field detection. **b** Original voltage signal generated by the AFG to simulate the corona current. **c** Response of the magnetometer with a microdisk radius of 205 μ m. The red (blue) curve shows the AC component of the optical transmission with (without) the signal

the blue curve represents the noise background without the pulsed current signal. In these results, the DC component of the optical transmission of the magnetometer has been filtered out. The measured response of the magnetometer exhibits excellent consistency with the original signal, with a slight distortion in the waveform, which originates from the varied cavity response for magnetic fields of different frequencies (see Fig. 3e). By performing a fast Fourier transform to both the measured response and noise, the time-domain response can be converted to the frequency domain, as displayed in Fig. S5 in the Supplemental Information. It can be seen that the corona current has a wide frequency distribution. With an RBW of 1 kHz, our magnetometer can measure the corona current at 2.5 MHz with an amplitude SNR of 30 dB (see Section 5 in Supplementary Information). This

demonstrates the potential of our magnetometers for corona current characterization in the real application scenario. The bandwidth of the magnetometer could be further improved by increasing the optical quality factor of the microcavity and the incident laser power, facilitating more accurate measurement of the corona current.

Discussion

In conclusion, we propose and fabricate a new type of mass-produced MCOM that exhibits ultrahigh sensitivity, by sputter coating a thin film of magnetostrictive material FeGaB onto the SiO₂ microdisk cavity. Through theoretical analysis, we derive the expression for photocurrent detected by the photodetector and noise-limited sensitivity using the intensity modulation readout mechanism, considering the laser frequency detuning. To optimize the sensitivity of our magnetometer, we conduct a comprehensive study on the relationship between the sensitivity and various parameters, including the optical detuning between the laser and the optical mode, as well as the geometric parameters of the FeGaB film and the SiO₂ microdisk. We experimentally fabricate multiple magnetometers with different radii (105 μm, 155 μm, 205 μm, 305 μm, 355 μm, and 405 μm) and characterize their sensitivities. We achieve an impressive minimum detectable magnetic field of 1.68 pT Hz^{-1/2} at 9.52 MHz, which is two orders of magnitude better than previous mass-produced magnetometers³⁷. Finally, we simulate the corona current in the high-voltage transmission line and successfully detect the pulsed magnetic field generated by this current using the fabricated magnetometers.

Utilizing the FeGaB material in our magnetometers to convert magnetic field signals into measurable mechanical signals represents a significant breakthrough. The peak sensitivity achieved in this work is the highest reported thus far in MCOM, making FeGaB a promising material for enhancing magnetometer sensitivity. Additionally, exploiting the delta-E effect (Young's modulus change in the presence of strain)⁶⁴ of the FeGaB film can further improve sensitivity in the low-frequency range. Besides, the anisotropic magnetization of the FeGaB film of our MCOM produces different responses to magnetic fields along the easy and hard axes, which could be utilized to detect the vector magnetic field. By carefully calibrating the magnetometer's responsivities to magnetic fields along *x*, *y*, and *z* directions, it is possible to determine the vector components of the magnetic field (*B_x*, *B_y*, *B_z*). Further developments can aim towards fully integrated MCOM using integrated silicon nitride ring resonators incorporated with FeGaB films, which are compatible with CMOS foundries. These CMOS-compatible, high-sensitivity magnetometers open up new possibilities for various applications, such as corona current detection, magnetic induction tomography and magnetoencephalography. In

applications of magnetic induction tomography and magnetoencephalography, an array of high-performance magnetometers can be utilized to measure the magnetic fields at different locations simultaneously, greatly reducing the time required for scanning.

Materials and methods

Deposition of the FeGaB film

To characterize the magnetic properties of magnetostrictive material, we sputter the FeGaB film onto a blank silica substrate. As a first step, a 5-nm-thick Ta layer is deposited to improve the adhesion between the FeGaB film and the silica substrate. Subsequently, a layer of FeGaB with a thickness of 1 μm is sputtered using a target with a composition of (Fe₈₀Ga₂₀)₈₈B₁₂. A radio frequency (RF) power of 100 W yields a sputtering rate of 0.13 nm s⁻¹ with an Ar pressure of 0.5 Pa. During the deposition, a static magnetic field of about 300 Oe is applied in the plane of the FeGaB film to induce a uniaxial in-plane anisotropy. Finally, a 5-nm-thick Ta cap layer is sputtered on top of the FeGaB film to prevent it from oxidation.

Fabrication of the magnetometer

The magnetometer is fabricated as follows. Starting with a 4-inch silicon wafer with a 1-μm-thick thermally oxidized silica on top, we pattern the SiO₂ microdisks using photolithography with a positive photoresist S1813 (step i). The pattern is then transferred to the oxide layer through inductively coupled plasma (ICP) etching utilizing a CHF₃/Ar/H₂ chemistry (step ii). Subsequently, a negative photoresist AZ nLOF 2070 is spin-coated onto the wafer, and a second photolithography process is performed to define the region for FeGaB deposition while protecting the perimeter of each disk (step iii). A stacked layer of Ta/FeGaB/Ta films, with thicknesses of 5 nm/1.3 μm/5 nm, is sputter coated on the surface of the SiO₂ microdisk (step iv). The size of the chip for FeGaB film sputtering is 27 mm × 27 mm, which is currently limited by the substrate size of our sputtering machine. It is possible to do sputter coating on an entire 4-inch wafer, by choosing a suitable sputtering machine. The excess Ta and FeGaB on the photoresist are removed through a lift-off process using Remover PG (step v). Finally, the silicon substrate is etched using XeF₂ to form a silicon pedestal, leaving the SiO₂ microdisk suspended (step vi). In the XeF₂ etching process, the FeGaB film is protected by the Ta cap layer from reacting with XeF₂.

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Author contributions

B.-B.L. conceived the idea. Z.-G.H., Y.-M.G., and J.-F.L. fabricated the devices and implemented the measurements. J.-W.C., Y.-C.L., C.-Q.H., J.L., and Z.L. helped with the sputter coating of the FeGaB films. Z.-G.H. and J.-F.L. performed the numerical simulations. B.-B.L., Z.-G.H., Y.-M.G., and J.-F.L. discussed the results and wrote the manuscript. All authors participated in the manuscript revision, reviewed the final draft, and gave their approvals for submission.

Data availability

The data that support the plots within this paper and other findings of this study are available from the corresponding authors upon request.

Conflict of interest

The authors declare no competing interests.

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References

- Zhao, N. et al. Sensing single remote nuclear spins. *Nat. Nanotechnol.* **7**, 657–662 (2012).
- Safronova, M. et al. Search for new physics with atoms and molecules. *Rev. Mod. Phys.* **90**, 025008 (2018).
- Savukov, I. & Karaulanov, T. Magnetic-resonance imaging of the human brain with an atomic magnetometer. *Appl. Phys. Lett.* **103**, 043703 (2013).
- Xiao, W. et al. A movable unshielded magnetocardiography system. *Sci. Adv.* **9**, eadg1746 (2023).
- Pizzo, F. et al. Deep brain activities can be detected with magnetoencephalography. *Nat. Commun.* **10**, 971 (2019).
- Edelstein, A. Advances in magnetometry. *J. Phys. Condens. Matter* **19**, 165217 (2007).
- Li, Y. et al. Nondestructive inspection and imaging of magnetic hydrogel using the alternating magnetic field infrared thermography. *Infrared Phys. Technol.* **131**, 104681 (2023).
- Wickenbrock, A. et al. Magnetic induction tomography using an all-optical ⁸⁷Rb atomic magnetometer. *Opt. Lett.* **39**, 6367–6370 (2014).
- Wickenbrock, A. et al. Eddy current imaging with an atomic radio-frequency magnetometer. *Appl. Phys. Lett.* **108**, 183507 (2016).
- Hagh, A. K. A., Ashtiani, S. J. & Akmal, A. A. S. A wideband, sensitive current sensor employing transimpedance amplifier as interface to Rogowski coil. *Sens. Actuators A Phys.* **256**, 43–50 (2017).
- Lopez, J. D. et al. Fiber-optic current sensor based on FBG and Terfenol-D with magnetic flux concentration for enhanced sensitivity and linearity. *IEEE Sens. J.* **20**, 3572–3578 (2020).
- Chen, G. Y. & Newson, T. P. Detection bandwidth of fibre-optic current sensors based on Faraday effect. *Electron. Lett.* **50**, 626–627 (2014).
- Xin, E. C. & Yuan, H. W. Development of a sensor for corona current measurement under high-voltage direct-current transmission lines. *Int. J. Distrib. Sens. Netw.* **12**, 1550147716664243 (2016).
- Yuan, H. W. et al. Development and application of high-frequency sensor for corona current measurement under ultra high-voltage direct-current environment. *IEEE Trans. Instrum. Meas.* **61**, 1064–1071 (2012).
- Tschirhart, C. L. et al. Imaging orbital ferromagnetism in a moiré Chern insulator. *Science* **372**, 1323–1327 (2021).
- Dang, H. B., Maloof, A. C. & Romalis, M. V. Ultrahigh sensitivity magnetic field and magnetization measurements with an atomic magnetometer. *Appl. Phys. Lett.* **97**, 151110 (2010).
- Maze, J. R. et al. Nanoscale magnetic sensing with an individual electronic spin in diamond. *Nature* **455**, 644–647 (2008).
- Bucholtz, F., Dagenais, D. M. & Koo, K. P. High-frequency fibre-optic magnetometer with 70 fT/√Hz resolution. *Electron. Lett.* **25**, 1719–1721 (1989).
- Yang, J. N. et al. Enhanced emission from a single quantum dot in a microdisk at a deterministic diabolical point. *Opt. Express* **29**, 14231–14244 (2021).
- Ba, Q. et al. Conformal optical black hole for cavity. *eLight* **2**, 19 (2022).
- Xiang, C. et al. Laser soliton microcombs heterogeneously integrated on silicon. *Science* **373**, 99–103 (2021).
- Lei, Y. C. et al. Fully reconfigurable optomechanical add-drop filters. *Appl. Phys. Lett.* **121**, 181110 (2022).
- Chang, L., Liu, S. T. & Bowers, J. E. Integrated optical frequency comb technologies. *Nat. Photonics* **16**, 95–108 (2022).
- Liu, J. et al. Emerging material platforms for integrated microcavity photonics. *Sci. China Phys. Mech. Astron.* **65**, 104201 (2022).
- Jin, M. et al. 1/f-noise-free optical sensing with an integrated heterodyne interferometer. *Nat. Commun.* **12**, 1973 (2021).
- Zhi, Y. Y. et al. Single nanoparticle detection using optical microcavities. *Adv. Mater.* **29**, 1604920 (2017).
- Tang, S. J. et al. Laser particles with omnidirectional emission for cell tracking. *Light Sci. Appl.* **10**, 23 (2021).
- Li, B. B. et al. Single nanoparticle detection using split-mode microcavity Raman lasers. *Proc. Natl Acad. Sci. USA* **111**, 14657–14662 (2014).
- Yu, X. C. et al. Single-molecule optofluidic microsensor with interface whispering gallery modes. *Proc. Natl Acad. Sci. USA* **119**, e2108678119 (2022).
- Forstner, S. et al. Cavity optomechanical magnetometer. *Phys. Rev. Lett.* **108**, 120801 (2012).
- Forstner, S. et al. Ultrasensitive optomechanical magnetometry. *Adv. Mater.* **26**, 6348–6353 (2014).
- Yu, C. Q. et al. Optomechanical magnetometry with a macroscopic resonator. *Phys. Rev. Appl.* **5**, 044007 (2016).
- Li, B. B. et al. Quantum enhanced optomechanical magnetometry. *Optica* **5**, 850–856 (2018).
- Li, B. B. et al. Ultrabroadband and sensitive cavity optomechanical magnetometry. *Photonics Res.* **8**, 1064–1071 (2020).
- Zhu, J. G. et al. Polymer encapsulated microcavity optomechanical magnetometer. *Sci. Rep.* **7**, 8896 (2017).
- Colombano, M. F. et al. Ferromagnetic resonance assisted optomechanical magnetometer. *Phys. Rev. Lett.* **125**, 147201 (2020).
- Li, B. B. et al. Invited article: scalable high-sensitivity optomechanical magnetometers on a chip. *APL Photonics* **3**, 120806 (2018).
- Gotardo, F. et al. Waveguide-integrated chip-scale optomechanical magnetometer. *Opt. Express* **31**, 37663–37672 (2023).
- Schliesser, A. et al. High-sensitivity monitoring of micromechanical vibration using optical whispering gallery mode resonators. *N. J. Phys.* **10**, 095015 (2008).
- Yu, W. Y. et al. Cavity optomechanical spring sensing of single molecules. *Nat. Commun.* **7**, 12311 (2016).
- Buchmann, L. et al. Complex squeezing and force measurement beyond the standard quantum limit. *Phys. Rev. Lett.* **117**, 030801 (2016).
- Krause, A. G. et al. A high-resolution microchip optomechanical accelerometer. *Nat. Photonics* **6**, 768–772 (2012).
- Guzmán Cervantes, F. et al. High sensitivity optomechanical reference accelerometer over 10 kHz. *Appl. Phys. Lett.* **104**, 221111 (2014).
- Yang, H. et al. High-sensitivity air-coupled megahertz-frequency ultrasound detection using on-chip microcavities. *Phys. Rev. Appl.* **18**, 034035 (2022).
- Yang, H. et al. Micropascal-sensitivity ultrasound sensors based on optical microcavities. *Photonics Res.* **11**, 1139–1147 (2023).
- Tang, S. J. et al. Single-particle photoacoustic vibrational spectroscopy using optical microresonators. *Nat. Photonics* **17**, 951–956 (2023).
- Meng, J. W. et al. Dissipative acousto-optic interactions in optical microcavities. *Phys. Rev. Lett.* **129**, 073901 (2022).
- Dong, C. Z. et al. Characterization of magnetomechanical properties in FeGaB thin films. *Appl. Phys. Lett.* **113**, 262401 (2018).

49. Lou, J. et al. Soft magnetism, magnetostriction, and microwave properties of FeGaB thin films. *Appl. Phys. Lett.* **91**, 182504 (2007).
50. Lou, J. et al. Giant electric field tuning of magnetism in novel multiferroic FeGaB/Lead Zinc Niobate-Lead Titanate (PZN-PT) heterostructures. *Adv. Mater.* **21**, 4711–4715 (2009).
51. McRae, T. G. et al. Thermo-optic locking of a semiconductor laser to a microcavity resonance. *Opt. Express* **17**, 21977–21985 (2009).
52. Bowen, W. P. & Milburn, G. J. *Quantum Optomechanics* (CRC Press, Boca Raton, 2015).
53. Aspelmeyer, M., Kippenberg, T. J. & Marquardt, F. Cavity optomechanics. *Rev. Mod. Phys.* **86**, 1391–1452 (2014).
54. Bowen, W. P. & Yu, C. Q. Cavity optomechanical magnetometers. In *High Sensitivity Magnetometers* (eds Grosz, A., Haji-Sheikh, M. J. & Mukhopadhyay, S. C.) 313–338 (Springer, Cham, 2017).
55. Yu, Y. M. et al. Modelling of cavity optomechanical magnetometers. *Sensors* **18**, 1558 (2018).
56. Hathaway, K. B., Clark, A. E. & Teter, J. P. Magnetomechanical damping in giant magnetostriction alloys. *Metall. Mater. Trans. A* **26**, 2797–2801 (1995).
57. Mech, R. & Kaleta, J. Influence of Terfenol-D powder volume fraction in epoxy matrix composites on their magnetomechanical properties. *Acta Mech. Autom.* **11**, 233–236 (2017).
58. Javid, U. A. et al. Cavity optomechanical sensing in the nonlinear saturation limit. *Laser Photonics Rev.* **15**, 2100166 (2021).
59. Hu, Y. et al. Generation of optical frequency comb via giant optomechanical oscillation. *Phys. Rev. Lett.* **127**, 134301 (2021).
60. Schliesser, A. et al. Resolved-sideband cooling of a micromechanical oscillator. *Nat. Phys.* **4**, 415–419 (2008).
61. Krause, A. G. et al. Nonlinear radiation pressure dynamics in an optomechanical crystal. *Phys. Rev. Lett.* **115**, 233601 (2015).
62. Wang, P. & Zhang, G. X. The measurement method for corona discharge current under high-voltage environment. *IEEE Trans. Instrum. Meas.* **57**, 1786–1790 (2008).
63. Wang, C. et al. Pulse current of multi-needle negative corona discharge and its electromagnetic radiation characteristics. *Energies* **11**, 3120 (2018).
64. Spetzler, B. et al. Exchange biased delta-E effect enables the detection of low frequency pT magnetic fields with simultaneous localization. *Sci. Rep.* **11**, 5269 (2021).